Quiz 5 Solutions, Math 111, Section 2 (Vinroot)

As always, show all steps clearly in your solution.

A particle is moving along a line, with position at time t seconds given by  $s(t) = t^3 + t^2 - 3$ , where s(t) is measured in cm, positive direction is forwards, and  $t \ge 0$ .

(a): Find the equation giving the velocity, v(t), and acceleration, a(t), at time t, and find the velocity and acceleration after 1 second (include units).

**Solution:** We know v(t) = s'(t), and a(t) = v'(t) = s''(t). Then  $v(t) = \frac{d}{dt}(t^3 + t^2 - 3) = 3t^2 + 2t$  and  $a(t) = \frac{d}{dt}(3t^2 + 2t) = 6t + 2$ , where v(t) is in cm/sec and a(t) is in cm/sec<sup>2</sup>.

After 1 second, t = 1, so  $v(1) = 3(1^2) + 2(1) = 5$  cm/sec, and a(1) = 6(1) + 2 = 8 cm/sec<sup>2</sup>.

(b): Explain why the particle is never moving backwards and its velocity is never decreasing (remember we are only considering  $t \ge 0$ ).

**Solution:** Since "moving backwards" means that position is decreasing, this would occur when  $\frac{ds}{dt} = s'(t)$  is negative. But  $s'(t) = v(t) = 3t^2 + 2t \ge 0$  when  $t \ge 0$ .

Similarly, the velocity of the particle would be decreasing at time t if v'(t) < 0. However,  $v'(t) = a(t) = 6t + 2 \ge 0$  when  $t \ge 0$ . So the velocity is never decreasing.