

(a): Compute the following limit (if it exists), making your steps clear:  $\lim_{h \rightarrow 0} \frac{\frac{1}{3+h} - \frac{1}{3}}{h}$ .

$$\lim_{h \rightarrow 0} \frac{\frac{1}{3+h} - \frac{1}{3}}{h} = \frac{\frac{1}{3+0} - \frac{1}{3}}{0} = \frac{\frac{1}{3} - \frac{1}{3}}{0} = \frac{0}{0}$$

First get a common denominator, then simplify (See solutions)

This is undefined, so you can't sub in 0

Tells you that there could be a cancellation in the algebra

0/0

(b): Compute the following limit if it exists, and if it does not exist but is infinite, describe the infinite limit and explain (factor the denominator):

$$\lim_{x \rightarrow 1^-} \frac{x-4}{x^2-3x+2}$$

$$\lim_{x \rightarrow 1^-} \frac{x-4}{x^2-3x+2} = \lim_{x \rightarrow 1^-} \frac{x-4}{(x-2)(x-1)}$$

$$= \lim_{x \rightarrow 1^-} \frac{1-4}{(1-2)(1-1)}$$

$$= \frac{-2}{(-1)(-0.001)}$$

$$= \boxed{-\infty}$$

This is the right idea, but you can't say these things are equal

As written, this is undefined

0.999

Correct thinking

One of these is a number, but the other isn't, so it will make

Correct answer!

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