

1. Write each of the following complex numbers in the form  $a + bi$ .

(a):  $-12e^{i\pi/4}$       (b):  $e^{17i\pi} + 2e^{5i\pi/4}$

2. Let  $\alpha$  and  $\beta$  be real numbers. You will show here that  $e^{i\alpha}e^{i\beta} = e^{i(\alpha+\beta)}$  using Euler's formula ( $e^{i\theta} = \cos(\theta) + i\sin(\theta)$ ).

First write  $e^{i\alpha}$  and  $e^{i\beta}$  using Euler's formula, then multiply the expressions and expand the result to put it into standard form  $a + bi$ . That is, multiply out  $(\cos(\alpha) + i\sin(\alpha))(\cos(\beta) + i\sin(\beta))$ , and put all real terms together and all imaginary terms together. Then show you get the same result when applying Euler's formula to  $e^{i(\alpha+\beta)}$  by using the trigonometric angle sum formulas (which are  $\cos(\alpha + \beta) = \cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta)$  and  $\sin(\alpha + \beta) = \sin(\alpha)\cos(\beta) + \cos(\alpha)\sin(\beta)$ ).

3. Find the general solution to each of the following homogeneous linear differential equations with constant coefficients. Use WolframAlpha or another mathematical tool to factor the characteristic polynomial.

(a):  $y^{(5)} - 6y^{(4)} + 16y''' - 32y'' + 48y' - 32y = 0$

(b):  $y^{(5)} - 11y^{(4)} + 66y''' - 230y'' + 481y' - 507y = 0$