

Quiz 3 Solutions, Math 103 - Precalculus

1. Suppose  $f(x) = x^2 + 1$ , and  $g$  is a function such that  $g(1) = 2$ .

(a): What is the value of  $f(g(1))$ ?

Solution:  $f(g(1)) = f(2) = 2^2 + 1 = \boxed{5}$

(b): What is the value of  $g(f(0))$ ?

Solution:  $g(f(0)) = g(0^2 + 1) = g(1) = \boxed{2}$

(c): What is the range of  $f$  and why?

Solution: Since  $x^2 \geq 0$  for all real  $x$ , then  $x^2 + 1 \geq 1$  for all real  $x$ . So the outputs of  $x$  are real numbers which are at least 1. Given any such  $y \geq 1$ , we have it as an output, since  $f(\sqrt{y-1}) = (\sqrt{y-1})^2 + 1 = y - 1 + 1 = y$ .

The range is all real  $y \geq 1$ .

2. Sketch a graph of  $y = 3^x - 2$ . Label axes, and label several points on the graph.

Solution:

$x$	$3^x - 2 = y$
0	$3^0 - 2 = -1$
1	$3^1 - 2 = 1$
2	$3^2 - 2 = 7$
-1	$3^{-1} - 2 = \frac{1}{3} - 2 = -\frac{5}{3}$

