

**Theorem** The standard power( $\beta$ ) distribution is a special case of the minimax( $\beta, \gamma$ ) distribution when  $\gamma = 1$ .

**Proof** Let  $X \sim \text{minimax}(\beta, \gamma)$ . The probability density function of  $X$  is

$$f_X(x) = \beta\gamma x^{\beta-1}(1-x^\beta)^{\gamma-1} \quad 0 < x < 1.$$

When  $\gamma = 1$ , this becomes

$$\begin{aligned} f_X(x) &= \beta x^{\beta-1}(1-x^\beta)^0 \\ &= \beta x^{\beta-1} \quad 0 < x < 1. \end{aligned}$$

which is the probability density function of a standard power( $\beta$ ) random variable.

**APPL verification:** The APPL statements

```
assume(beta > 0);
X := [[x -> beta * gamma * x ^ (beta - 1) * (1 - x ^beta) ^ (gamma - 1)],
      [0, 1], ["Continuous", "PDF"]];
subs(gamma = 1, %);
```

verify the result.